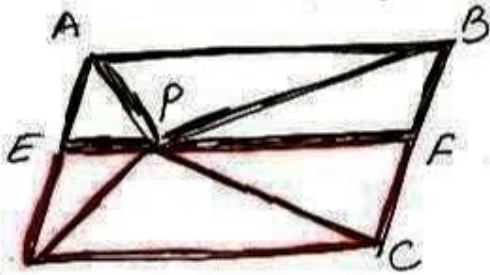


(4)



To prove - $\text{ar}(\triangle APB) + \text{ar}(\triangle PCD) = \frac{1}{2} \text{ar}(\text{ABCD})$
 $\text{ar}(\triangle APD) + \text{ar}(\triangle PBC) = \text{ar}(\triangle APB) + \text{ar}(\triangle PCD)$

Const - draw $EF \parallel DC$

Proof - $AD \parallel BC$ [Opp. sides of $\parallel gm$]
 $\Rightarrow DE \parallel CF$

$EF \parallel DC$

$\square DCFE$ is a $\parallel gm$

$EF \parallel DC, AB \parallel DC$

$\therefore EF \parallel AB$

$AD \parallel BC$

$AE \parallel BF$

$\square EFBA$ is a $\parallel gm$

$\text{ar}(\triangle PDC) = \frac{1}{2} \text{ar}(\parallel gm DCFE) \dots \textcircled{i}$
 $\text{ar}(\triangle APB) = \frac{1}{2} \text{ar}(\parallel gm EFBA) \dots \textcircled{ii}$ [Δ and $\parallel gm$
 on same base
 and between
 same parallel
 lines]

$\textcircled{i} + \textcircled{ii}$

$\text{ar}(\triangle APB) + \text{ar}(\triangle PCD) = \frac{1}{2} [\text{ar}(\parallel gm DCFE) + \text{ar}(\parallel gm EFBA)]$
 $= \frac{1}{2} \text{ar}(\parallel gm ABCD) \dots \textcircled{iii}$

Similarly $\text{ar}(\triangle APD) + \text{ar}(\triangle PBC) = \frac{1}{2} (\text{ar} \parallel gm ABCD) \dots \textcircled{iv}$

From \textcircled{iii} and \textcircled{iv} NCERT Exemplar Solutions by Dev Anoop (Bathinda)

$\text{ar}(\triangle APD) + \text{ar}(\triangle PBC) = \text{ar}(\triangle APB) + \text{ar}(\triangle PCD)$