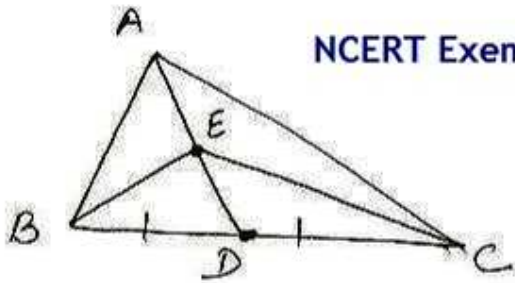


①



To prove  $\text{ar}(\triangle ABE) = \text{ar}(\triangle ACE)$

Proof  $\text{ar}(\triangle ABD) = \text{ar}(\triangle ACD)$  ... ① [Median divides a  $\Delta$  into 2  $\Delta$ s equal in area]

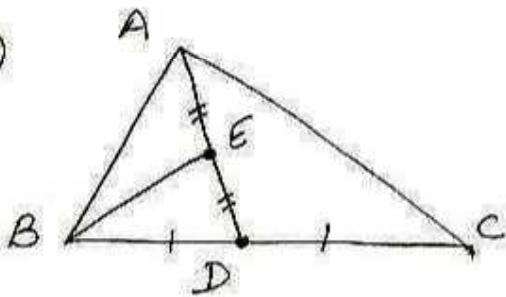
$$\text{ar}(\triangle EBD) = \text{ar}(\triangle ECD) \dots \text{②} \quad (\text{do})$$

$$\text{①} - \text{②}$$

$$\text{ar}(\triangle ABD) - \text{ar}(\triangle EBD) = \text{ar}(\triangle ACD) - \text{ar}(\triangle ECD)$$

$$\Rightarrow \text{ar}(\triangle ABE) = \text{ar}(\triangle ACE)$$

②



To show  $\text{ar}(\triangle BED) = \frac{1}{4} \text{ar}(\triangle ABC)$

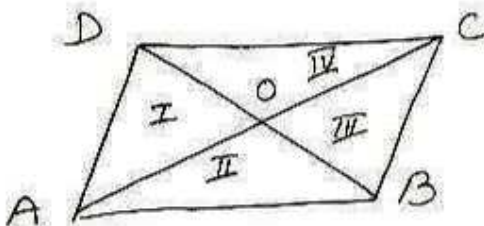
Proof  $\text{ar}(\triangle ABD) = \frac{1}{2} \text{ar}(\triangle ABC)$  ... ① [Median divides a  $\Delta$  into 2  $\Delta$ s equal in area]

$$\text{ar}(\triangle BED) = \frac{1}{2} \text{ar}(\triangle ABD) \dots \text{②} \quad (\text{do})$$

From ① and ②

$$\text{ar}(\triangle BED) = \frac{1}{4} \text{ar}(\triangle ABC)$$

③



To prove  $\text{ar}(\triangle I) = \text{ar}(\triangle II) = \text{ar}(\triangle III) = \text{ar}(\triangle IV)$

Proof diagonals of a ||gm bisect each other

$$\therefore OA = OC, OB = OD$$

In  $\Delta DAC$ , DO is median to side AC [  $OA = OC$  ]

$$\therefore \text{ar}(\triangle I) = \text{ar}(\triangle IV) \dots \text{①}$$

$$\text{Sim. } \text{ar}(\triangle IV) = \text{ar}(\triangle III) \dots \text{②}$$

$$\text{ar}(\triangle III) = \text{ar}(\triangle II) \dots \text{③}$$

From ①, ②, ③

$$\text{ar}(\triangle I) = \text{ar}(\triangle II) = \text{ar}(\triangle III) = \text{ar}(\triangle IV)$$