

To show $\triangle ABM \cong \triangle PQN$
 $\triangle ABC \cong \triangle PQR$

Proof $BC = QR$
 $\frac{1}{2}BC = \frac{1}{2}QR$
 $\Rightarrow BM = QN$ [as medians to sides BC, QR resp.]

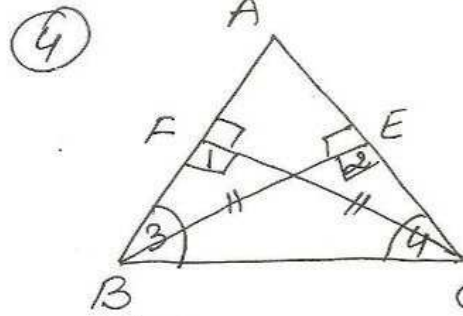
In $\triangle ABM$ and $\triangle PQN$
 $AB = PQ$ (given)
 $AM = PN$ (given)
 $BM = QN$ (proved)

$\therefore \triangle ABM \cong \triangle PQN$ by SSS prop

$\angle B = \angle Q$ (cpct)

In $\triangle ABC$ and $\triangle PQR$
 $AB = PQ$ (given)
 $\angle B = \angle Q$ (proved)
 $BC = QR$ (given)

$\therefore \triangle ABC \cong \triangle PQR$ by SAS prop



To prove $AB = AC$

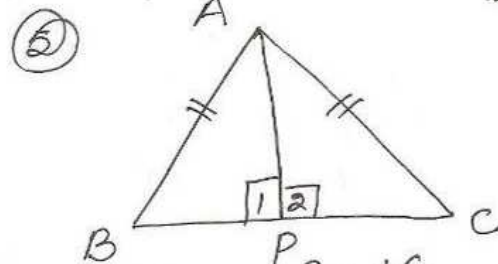
Proof In $\triangle BFC$ and $\triangle CEB$

$\angle 1 = \angle 2 = 90^\circ$
 $BC = CB$ (common)
 $CF = BE$ (given)

$\therefore \triangle BFC \cong \triangle CEB$ by RHS prop

$\angle 3 = \angle 4$ (cpct)

$\Rightarrow AC = AB$ (converse of isos \triangle prop)



To show $\angle B = \angle C$

Proof In $\triangle APB$ and $\triangle APC$

$\angle 1 = \angle 2 = 90^\circ$
 $AB = AC$
 $AP = AP$

$\therefore \triangle APB \cong \triangle APC$ by RHS prop

$\angle B = \angle C$ (cpct)