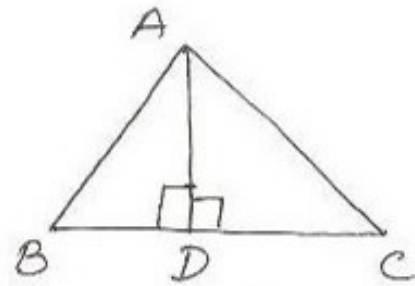


(16)

given - In $\triangle ABC$
 $AB = BC = CA$,
 $AD \perp BC$



to prove $3AB^2 = 4AD^2$

proof - In $\triangle ABC$, $AD \perp BC$

$\therefore BD = CD$ --- (i) [In an equilateral triangle altitude is also median]

In rt $\triangle ADB$

$$AB^2 = AD^2 + BD^2 \quad \text{[Pythagoras Theorem]}$$

$$= AD^2 + \left(\frac{BC}{2}\right)^2 \quad \text{[Using (i)]}$$

$$AB^2 = AD^2 + \frac{BC^2}{4}$$

$$AB^2 = AD^2 + \frac{AB^2}{4} \quad \text{[Since } AB = BC \text{]}$$

$$\times 4 \Rightarrow 4AB^2 = 4AD^2 + AB^2$$

$$\Rightarrow 3AB^2 = 4AD^2$$

(17)

$$AC^2 = 12^2$$

$$= 144$$

$$AB^2 + BC^2 = (6\sqrt{3})^2 + 6^2$$

$$= 108 + 36$$

$$= 144$$

$$\therefore AC^2 = AB^2 + BC^2$$

$$\angle B = 90^\circ \text{ (C)}$$

[Converse of Pythagoras Theorem]

