

1(i) $A(2, 3), B(-1, 0), C(2, -4)$
 $\text{ar}(\triangle ABC)$
 $= \frac{1}{2} |2(0+4) + (-1)(-4-3) + 2(3-0)|$
 $= \frac{1}{2} |2 \times 4 - 1(-7) + 2 \times 3|$
 $= \frac{1}{2} |8 + 7 + 6|$
 $= \frac{21}{2} \text{ sq. units}$

1(ii) $A(-5, -1), B(3, -5), C(5, 2)$
 $\text{ar}(\triangle ABC)$

$$\begin{aligned} &= \frac{1}{2} \begin{vmatrix} -5 & -1 \\ 3 & -5 \\ 5 & 2 \\ -5 & -1 \end{vmatrix} \\ &= \frac{1}{2} [(-5)(-5) - 3(-1) + 3 \times 2 - 5(-5) \\ &\quad + 5(-1) - (-5)2] \\ &= \frac{1}{2} |25 + 3 + 6 + 25 - 5 + 10| \\ &= \frac{1}{2} \times 64 \\ &= 32 \text{ sq. units} \end{aligned}$$

2(i) $A(7, 2), B(5, 1), C(3, k)$
 $\text{Pts } A, B, C \text{ are collinear}$
 $\therefore \text{ar}(\triangle ABC) = 0$

$$\begin{aligned} &\frac{1}{2} [7(1-k) + 5(k+2) + 3(-2-1)] = 0 \\ &7 - 7k + 5k + 10 - 9 = 0 \\ &\Rightarrow -2k = -8 \\ &\Rightarrow k = \frac{-8}{-2} \\ &\Rightarrow k = 4 \end{aligned}$$

2(ii) $A(8, 1), B(k, -4), C(2, -5)$
 $\text{Pts } A, B, C \text{ are collinear}$
 $\therefore \text{ar}(\triangle ABC) = 0$
 $\frac{1}{2} [8(-4+5) + k(-5-1) + 2(1+4)] = 0$
 $\Rightarrow 8 \times 1 + k(-6) + 2 \times 5 = 0$
 $\Rightarrow 8 - 6k + 10 = 0$
 $\Rightarrow -6k = -18$
 $\Rightarrow k = \frac{-18}{-6}$
 $\Rightarrow k = 3$