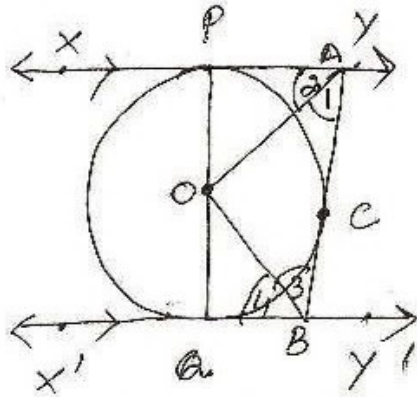


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To Prove $\angle AOB = 90^\circ$

Proof

$$\angle 1 = \angle 2$$

$$\angle 3 = \angle 4$$

[tangents from an external point are equally inclined to the line join. centre of O to external point]

$$XY \parallel X'Y'$$

$$\angle PAB + \angle QBA = 180^\circ$$

(co-interior angles)

$$\angle 1 + \angle 2 + \angle 3 + \angle 4 = 180^\circ$$

$$\angle 1 + \angle 1 + \angle 3 + \angle 3 = 180^\circ$$

($\because \angle 1 = \angle 2$
 $\angle 3 = \angle 4$)

$$2(\angle 1 + \angle 3) = 180^\circ$$

$$\Rightarrow \angle 1 + \angle 3 = 90^\circ$$

adding $\angle AOB$ on both sides

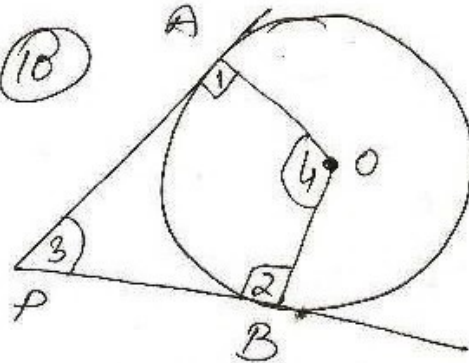
$$\angle 1 + \angle 3 + \angle AOB = 90^\circ + \angle AOB$$

$$\Rightarrow \angle AOB = 180 - 90$$

(angle sum prop. of Δ)

$$= 90^\circ$$

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To Prove

$$\angle APB + \angle AOB = 180^\circ$$

Proof

$$\angle 1 = \angle 2 = 90^\circ$$

In $\square PBOA$

$$\angle 1 + \angle 2 + \angle 3 + \angle 4 = 360^\circ$$

(angle sum prop. of \square)

$$90^\circ + 90^\circ + \angle 3 + \angle 4 = 360^\circ$$

$$\Rightarrow \angle 3 + \angle 4 = 360 - 180$$

$$\Rightarrow \angle APB + \angle AOB = 180^\circ$$