

to prove $\frac{AB}{PQ} = \frac{AD}{PM}$

proof $\triangle ABC \sim \triangle PQR$

$$\Rightarrow \frac{AB}{PQ} = \frac{BC}{QR}$$

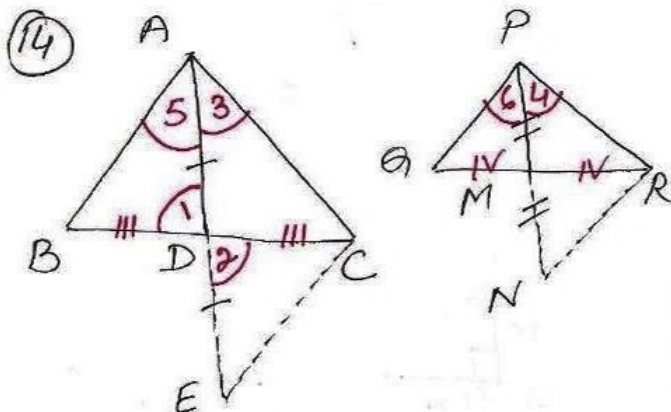
$$\Rightarrow \frac{AB}{PQ} = \frac{BD}{QM}$$

[D is midpt of BC, M is midpt of QR]

and $\angle B = \angle Q$

$\therefore \triangle ABD \sim \triangle PQM$
by SAS Sim.

$$\Rightarrow \frac{AB}{PQ} = \frac{AD}{PM}$$



to prove $\triangle ABC \sim \triangle PQR$
Const. - Produce AD to E
s.t. $DE = AD$, join EC
produce PM to N, s.t.
 $MN = PN$ join NR

proof $AD = ED$ (by const)
 $\angle 1 = \angle 2$ (vertically opposite \angle s)

$BD = CD$ (\because AD is median to side BC of $\triangle ABC$)

$\therefore \triangle ADB \cong \triangle EDC$ by SAA congruence

$$AB = EC \text{ (c.p.c.t.)}$$

Similarly $PQ = NR$

$$\frac{AB}{PQ} = \frac{AC}{PR} = \frac{AD}{PM}$$

$$\frac{EC}{NR} = \frac{AC}{PR} = \frac{2AD}{2PM} \text{ [}\because AB=EC, PQ=NR\text{]}$$

$$\frac{EC}{NR} = \frac{AC}{PR} = \frac{AE}{PN} \text{ [}\because AD=DE, PM=MN\text{]}$$

$\therefore \triangle AEC \sim \triangle PNR$ by SSS Sim.

$$\Rightarrow \angle 3 = \angle 4 \dots \text{ (i)}$$

Similarly $\angle 5 = \angle 6 \dots \text{ (ii)}$

$$\text{(i) + (ii)} \quad \angle 3 + \angle 5 = \angle 4 + \angle 6$$

$$\Rightarrow \angle BAC = \angle QPR$$

and $\frac{AB}{PQ} = \frac{AC}{PR}$

$\therefore \triangle ABC \sim \triangle PQR$ by SAS congruency